Abstract

We develop a model of vertical pricing in which an original manufacturer sets wholesale prices in two markets integrated at the distributor level by parallel imports. We show that if competition policy requires uniform wholesale prices across locations, retail prices could be higher than those induced without such a restriction. However, retail prices would tend to converge as transportation costs fall, generating a complementarity between competition policy and market integration at low trade costs. Overall, a per se rule banning wholesale price discrimination is not optimal for consumer welfare in comparison with a rule of reason approach.

Keywords: Vertical Restraints; Parallel Imports; Market Integration; Price Discrimination; Competition Policy

JEL Codes: F15, L14, K21
1 Introduction

Competition policy aims to encourage competition among firms, which should achieve maximum consumer benefits. A prominent example is restrictions against price discrimination across customers. Another is permission of parallel imports (PI), which are goods placed legitimately onto the market in one country but subsequently imported into another country without the authorization of the holder of intellectual property rights (IPR) in the latter market. This form of arbitrage is presumed to integrate markets and enhance competition, again to the benefit of consumers. In this paper, however, we show that in the common case where goods are distributed across borders in a vertical relationship between an original manufacturer, which owns IPR, and independent distributors with market power, policy restraints on price discrimination at the wholesale level in the presence of parallel trade can raise retail prices compared to the unconstrained equilibrium. In other words, parallel trade integrates markets but strategic responses to pricing constraints can harm consumer welfare. Thus, there are circumstances in which consumer gains and market integration can come into conflict.

The legality of parallel imports depends on the point at which the original manufacturer’s rights to control redistribution are exhausted under the law. The European Union (EU) has a policy of regional exhaustion, which states that PI are impermissible from outside the community but first sale of a good anywhere within its territory, whether to distributors or final consumers, ends the originator’s distribution rights. The U.S. policy of national exhaustion is essentially the same because redistribution rights are ended upon first sale anywhere within the country. Thus, parallel trade across countries within the EU, and gray-market trade between regional territories within the United States, are seen as a key form of integrating markets through legal arbitrage.

In particular, as discussed next, EU case law rigorously defends the single market both by discouraging wholesale price discrimination across markets and upholding the ability of companies to engage in arbitrage. The United States is more lenient toward price differentiation, but still limits its scope in order to preserve competition, while preserving the right to within-nation arbitrage. This policy mix sets up a number of strategic decisions for the IPR holder, which wishes to limit parallel trade, reduce competition among distributors, and induce optimal retail prices. To analyze these tradeoffs we set out a model in which an original manufacturer has at its disposal just two instruments,
the wholesale prices it can charge its independent distributors in two different markets. The flexibility to set differentiated distributor prices is central in managing the problems arising from parallel trade. A policy requiring uniform wholesale charges reduces the number of instruments from two to one, making the task more difficult for the manufacturer and potentially raising inefficiencies on the retail markets.

In this framework we derive two novel results. First, there are relevant market circumstances under which a policy requiring uniform wholesale prices generates higher retail prices in both markets than would be the case with discriminatory prices. The idea that restraints against price discrimination can reduce consumer welfare by reducing sales in a low-price market is familiar from prior literature (Varian 1998, Malueg and Schwartz 1994). However, this possibility arises here in a quite different context from simple retail arbitrage. Moreover, our model has the novel feature that prices can rise in both markets as a result of competition policy, rather than solely in the lower-price location.

Second, as markets become increasingly integrated a complementarity arises between uniform pricing and efforts to reduce trade costs facing arbitragers. Specifically, a requirement of common wholesale prices under legal PI becomes advantageous for consumer welfare as trade costs are reduced to low levels. Taken together, these two results imply that the welfare impacts of a uniform wholesale price depend on market circumstances. Since trade costs vary across products and markets, it would seem that a per se ban on price discrimination should be replaced by a rule of reason.

These differences from standard theory arise because distributor-level arbitrage under vertical price control is different from retail-level arbitrage alone. For example, it is possible with vertical pricing for PI to flow from a country where retail price is higher to a market where it is lower (Chen and Maskus 2005). Regarding the analysis here, a uniform wholesale price does not imply a uniform retail price in a vertical model with market power. Indeed, it is possible in this setup for retail prices to diverge under market integration (Ganslandt and Maskus 2007). Thus, analysis of the effects of rules regarding price discrimination needs to account for the structure of distribution markets.

1.1 Policy and Case Law

To motivate our analysis we describe the basic laws and legal findings regarding price discrimination as it may affect the scope for parallel trade. Competition
law in the EU aims at both encouraging competition among firms and protecting the unimpeded functioning of the single market. The latter goal is achieved by reducing the costs of intra-market trade and safeguarding the legality of arbitrage through PI. Firms are permitted neither to partition the European market nor to discriminate among consumers based on their nationality or location. Both objectives generally are seen to be in concert with one another.

A potential conflict arises because parallel trade emerges from international price differences, which could exist at the wholesale level due to the strategic decisions of IPR holders. At the same time, EU law prohibits certain types of price discrimination by a monopolist, specifically if the strategy puts one trading partner (e.g., a distributor or parallel trader) at a competitive disadvantage. Article 82 of the EC Treaty states that price discrimination of this kind is abusive and illegal per se. Pricing that is harmful to the single market is considered to be a particularly serious infringement of Article 82 and prices charged to prevent or limit the scope for PI are condemned.

The relevant European case law can be summarized in three principles (Whish, 2003). First, the British Leyland (BL) case established that a monopolist cannot charge excessive prices or fees to impede PI.\footnote{See 84/379/EEC: Commission Decision of 2 July 1984 relating to a proceeding under Article 86 of the EEC Treaty (IV/30.615 - BL).} Beginning in 1981 BL refused to certify imported automobiles of its manufacture for use on British roads, then later charged a fee of 150 pounds sterling for a certificate of conformity, whereas it charged 25 pounds sterling for a domestically purchased car. The European Commission found that BL abused its dominant position, both in refusing certification and charging differentially higher fees to PI firms. Because the fees impeded parallel trade they were deemed illegal.

Second, a monopolist can discriminate in prices across geographical markets only to a limited extent and the difference in prices must be "objectively" justified by cost conditions. This principle stems from Article 82, which states that an abuse of dominant position may consist in "directly or indirectly imposing unfair purchasing or selling prices to other companies." In United Brands the European Court of Justice (ECJ) ruled that the defendant acted illegally by charging different prices to distributors depending on the final destination of its product.\footnote{Case 27/76, United Brands, ECR 207, 1978.} In particular, United Brands Company (UBC) sold bananas in bulk to distributors in various member states at two central locations (Rotterdam and Bremerhaven), charging different prices to wholesalers from different coun-
tries. UBC argued that those prices were justified by being directly linked to final market prices for bananas in each country. The ECJ found that UBC was entitled to take local market conditions into account only to a limited extent, for the risks arising from local market conditions were borne by local distributors and retailers, whereas UBC was selling a homogeneous product in a centralized location. Thus, charging segmented prices based on geographical location was an abuse of pricing power and limited cross-border trade.

In a later case the Court held that, because of the practical difficulty of computing production costs, an assessment of abuse could be made by comparing the prices charged for the same product or service on other geographic markets, an item of direct relevance for PI.\(^3\) Similarly, the Court found that the considerable price discrimination across member states undertaken by a dominant firm in materials for packaging liquid foods was an abuse of position and incompatible with the single market.\(^4\) It could not be objectively attributed to market conditions because the relevant market was the entire EU and transport costs were low. Thus, the price discrimination was found to be a strategy to partition markets, violating Article 82.

Third, it is illegal for a monopolist to practice price discrimination by granting rebates to distributors in a way that impedes growth of competition.\(^5\) In particular, the discriminatory "border rebates" offered to customers located close to the Northern Ireland border were found to put those who did not qualify for them at a competitive disadvantage. According to the ECJ, rebates that limit competition from imports or exports are incompatible with Article 82. Similarly, the European Commission found that a rebate applying only to Michelin tires purchased from one distributor (Michelin France) impeded access of the company’s distributors in other EU countries to the French market.\(^6\) Thus, rebates designed by a dominant firm to discourage cross-border purchases within the EU are illegal.

Turning to the United States, the legality of price discrimination is based on the Robinson-Patman Act of 1936 and subsequent guidelines issued by the Federal Trade Commission (FTC). In essence, this act bars setting price differences across customers if doing so constitutes an anti-competitive practice that

\(^3\)Case 395/87, Tournier, ECR 1988.
\(^4\)Case ECR I-5951, Tetra Pak II, November 1996.
\(^5\)Case T-228/97, Irish Sugar plc, October 1999.
injures competition. In subsequent interpretation, the courts have clarified that conditions of competition are paramount and that price discrimination arising from legitimate cost differences or otherwise not interfering with other antitrust principles is permissible. The Supreme Court has recognized that overly strict interpretations of Robinson-Patman could result in price uniformity and rigidity that itself may cause problems for competition.\(^7\)

This stance implies that price differentiation is likely to run afoul of the courts primarily where it threatens to injure competition. In the principal case to date, a tobacco company was accused of violating the law by giving volume discounts for generic cigarettes to some wholesalers and not to others, because those discounts could reduce distributor costs in a predatory way and drive distributors of other tobacco firms out of business.\(^8\) While stipulating again that such price setting might be illegal, the Supreme Court found for the defendant because the plaintiff could not demonstrate a causal link to reduced competition and injury.

In a case similar to that involving UBC in the EU, the Supreme Court ruled that for an original firm to charge different wholesale (or retail) prices to its distributors (retail stores), it must be able to demonstrate with rigorous accounting that the price differential precisely reflects the additional costs of selling to varying customers.\(^9\) In this case Texaco sold gasoline to two distributors at a price lower than that charged to 12 independent retailers in a particular locality. The Supreme Court found that the company could not demonstrate a compelling cost-based reason for doing so and that competition had been injured.

Thus, it is fair to say that U.S. authorities uphold a policy barring price discrimination at the distributor level unless manufacturers can demonstrate a cost-based reason for it, but only if there is demonstrable injury to competition. The EU takes a more rigorous stance against such discrimination, though there remain exceptions (Geradin and Petit, 2007).

### 1.2 Model Summary

To capture the linkages between distributor-level PI, price discrimination and welfare we develop a model of integrated wholesale markets and vertical pricing. We analyze conditions under which the objective of market integration is com-

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\(^7\)Great Atlantic and Pacific Tea Co. v FTC, 440 U.S. 69 No. 77-564 (1979).
patible with the goal of raising consumer welfare and conditions under which it is not. We are particularly interested in the issue of wholesale price discrimination and the effects it has on arbitrage between territories and retail prices. The situation we have in mind involves a manufacturing firm with monopoly rights to distribute some good over which it owns IPR in two markets. This firm sets non-linear prices, in the form of two-part tariffs, to its distributors in these countries. Because these prices are the control instruments available for the firm, their profit-maximizing levels likely are different across markets. Thus, the manufacturer has an incentive to discriminate in prices at the distributor level, a strategy that can reduce the volume of trade through parallel channels.

We explore the impact of permitting PI in the presence of wholesale price discrimination, on the one hand, and uniform pricing, on the other hand. We show that a policy requiring the manufacturing firm to charge nondiscriminatory prices can result in retail prices that are higher in all markets compared to an equilibrium with price discrimination. More precisely, we demonstrate that, for a relevant range of trade costs, consumers in both markets can benefit jointly if policy permits the manufacturing firm to price discriminate among distributors. However, this result depends on the level of trade costs and we show that efforts to push such costs to low levels through market integration can complement a uniform-pricing policy in terms of consumer welfare.

The paper is organized as follows. In Section 2 we present our model and in Section 3 we undertake theoretical analysis of the various policy regimes with one-way parallel trade. In Section 4 we summarize the welfare implications. In Sections 5 and 6 we consider a number of relevant model extensions, including analysis of two-way parallel trade. Concluding remarks are offered in Section 7.

2 A Theoretical Model of Cross-border Trade

Our model builds on earlier work analyzing PI in a model of vertical price control. This approach was first set out by Maskus and Chen (2002) and Chen and Maskus (2005) and further developed by Ganslandt and Maskus (2007). They develop a simple model of vertical price control in which an original manufacturer sets wholesale prices to either one or two distributors, with the possibility of PI from one market to the other. As noted in those papers there are three

essential efficiency trade-offs in this model. The manufacturer has to balance
the losses from a pro-competitive price effect of parallel imports, the resource
costs wasted in the activity of cross-border trade, and the double-markup prob-
lem in inducing a profit-maximizing retail price in the export market. Empirical
evidence in Maskus and Chen (2002) and Ganslandt and Maskus (2003) points
to vertical control problems as an important determinant of parallel trade.\footnote{\textsuperscript{11}A study by National Economic Research Associates (1999) reported survey evidence of
significant flows of parallel trade within the European Union in the early 1990s. While the
report tended to focus on retail price differences, it pointed out that the bulk of parallel trade
happens at the wholesale or distributor level.}

Perhaps the most closely related study is by Matsumura (2003). Using a
spatial location model, he found that an upstream monopolist wishes to limit
competition between two downstream duopolists by using exclusive territories.
However, the existence of exclusive territories actually reduces final-product
prices in local markets when distributors compete in quantities, because it in-
duces lower wholesale prices in the first place.\footnote{\textsuperscript{12}Ra\"ıf and Schmidt (2005) analyze the implications of exclusive territories used by firms
in international trade. They concluded that trade liberalization may lead manufacturers
to offset the loss of tariff barriers with contracts imposing exclusive territories, which may
decrease competition and welfare.}

In the model that follows we extend the vertical price control framework to
consider the implications of competition-policy restrictions on pricing imposed
on the manufacturer. While we describe the model generally in terms of EU ex-
haustion policy permitting PI across national borders, the insights apply equally
to gray-market trade across exclusive territories within the United States.

We begin with basic assumptions. A manufacturer, $M$, sells its product in
two markets, called $A$ and $B$. Firm $M$ sells its product through an independent
exclusive distributor in each market. The demand in market $A$ is

$$X(p_A) = 1 - p_A,$$  \hspace{1cm} (1)

and that in $B$ is

$$Y(p_B) = S(1 - bp_B).$$  \hspace{1cm} (2)

It is assumed throughout the paper that demand in market $B$ is more price-
elastic than demand in market $A$, i.e. $b \geq 1$. It is also assumed that market
$B$ is sufficiently large, i.e. $S$ is above some threshold level $S_c$, to ensure that it
is profitable for the manufacturing firm to serve both markets in equilibrium.\footnote{\textsuperscript{13}The critical market size $S_c$ solves the following equation:
$$1 - 3bc^2 - 10bc - 565c + 135c^2 + 10bc^2 - 80c + 45c^2 - 18Sc + 9S - 10bc + 8c^2 + 4bc = \left(\frac{1}{2}\right)^2,$$
where the left-hand side is the lowest profit in an equilibrium in which the manufacturing firm

\section{Conclusion}
Manufacturer $M$ has a constant marginal cost of production, which is $c$. The marginal cost of retailing in both countries is normalized to zero. Retail markets are segmented through much of the analysis, though we consider retail arbitrage in an extension.\footnote{As argued in Ganslandt and Maskus (2007), this segmentation of consumer markets at the retail level can be motivated on several grounds. In some industries consumer arbitrage is illegal, while parallel trade at the wholesale level is permitted. This is the case with prescription drugs in the European Union for instance. In other industries, physical products and non-tradeable services are tied, causing effective market segmentation at the retail level. Local warranties bundled with capital goods and local plans bundled with cell phones are examples in this category. Finally, retail arbitrage can be prohibitively costly, while margins permit parallel trade at the wholesale level.}

Suppose that the manufacturing firm $M$ can offer the distributor in market $i$ ($i = A, B$) a familiar two-part tariff contract in the form of $(w_i, T_i)$, where $w_i$ is the wholesale price and $T_i$ is a transfer payment (franchise fee) from the distributor to $M$. The manufacturing firm cannot prevent either distributor from selling the product also in the other market, either directly or through intermediaries, such as firms specialized in parallel trade. That is, we assume that either $M$ cannot legally limit the distributor’s territory of sales, or it is too costly for $M$ to enforce any such constraint. The manufacturing firm can only control supply with wholesale prices. We rule out contracts that incorporate an agreement to limit the volume of parallel trade directly or indirectly.\footnote{As discussed by Ganslandt and Maskus (2007), such contracts would be illegal in the EU.}

With this setup, suppose that the distributor incurs an additional constant marginal cost $t \geq 0$ in selling the good in the market where it is not located. For instance, $t$ could be the transaction cost or the transportation cost. Finally, assume that if the distributor sells in the market where it is not located, it competes with the local distributor in a Cournot fashion. Let the quantities sold in $A$ by the two distributors be $x_A$ and $x_B$, respectively, and the quantity sold in $B$ be $y_A$ and $y_B$. Subscripts refer to the identity of the distributor. A subgame-perfect Nash equilibrium is two pairs $(x_A, x_B)$ and $(y_A, y_B)$ that constitute Nash equilibria for any $(w_i, T_i)$ for $i = A, B$, together with an optimal choice of $(w_i, T_i)$ for $i = A, B$ by the manufacturing firm. Let $w$ denote the vector $(w_A, w_B)$ and $T$ denote the vector $(T_A, T_B)$.

Our main objective is to analyze how the manufacturing firm sets the wholesale prices and the transfer payments to maximize its profit. The manufacturing firm’s profit is equal to total revenues in equilibrium minus real costs incurred. More precisely, the objective of the manufacturing firm (expressed in reduced serves both markets and the righ-hand side is the equilibrium profit from serving only market $A$.}
form\textsuperscript{16} is:

\[
\max \pi(w) = X (p_A(w)) (p_A(w) - c) + Y (p_B(w)) (p_B(w) - c) - t (y_A(w) + x_B(w)).
\]

where the first term on the right hand side is the operating profit in market \(A\), the second term is the operating profit in market \(B\) and the third term is the real cost of cross-border trade.

Initially we make the assumption that only distributor \(B\) can engage in cross-border trade. Consequently, distributor \(A\) can sell only in its home market while distributor \(B\) can choose to sell in both markets. Restricting our attention initially to one-way arbitrage simplifies the presentation significantly. Later we extend the analysis to permit two-way trade at the wholesale level. As we shall see this gives further insights but makes the analysis substantially more complex.

There are several possible situations in which only one-way trade is feasible. First, if there are fixed costs of wholesaling (not explicitly modeled here) and market \(B\) is small while market \(A\) is large, an asymmetry is possible, with products flowing from the small to the large country but not the other way around. Portugal and the United Kingdom within the European Union could exemplify this case. Second, there may be asymmetric product standards between the two countries. For example, software in English may be used in most countries while software in Danish is hard to use for any consumer outside Scandinavia. Third, the countries may vary in their legal treatment of PI, implying that such trade is permitted only in one direction. An example is that Australia is open to parallel imports of copyrighted goods while the European Union and the United States are not.

We derive the equilibrium of the model under two policy regimes. The first case is referred to as "discriminatory wholesale pricing". When discriminatory pricing is permitted, the manufacturing firm can set one different wholesale prices for the two distributors. The second case is referred to as "uniform wholesale pricing". In this case the manufacturing firm is required to charge the same wholesale price in both markets to ensure that neither distributor is put at a competitive disadvantage in relation to the other.

We assume that the marginal cost of production is sufficiently high to ensure

\[T_A = x_A (p_A - w_A) + y_A (p_B - w_B) - t y_A\] and \[T_B = x_B (p_A - w_A) + y_B (p_B - w_B) - t x_B.\]
that the manufacturing firm’s optimal wholesale price in equilibrium is positive\textsuperscript{17} and sufficiently low to ensure that there is positive demand in both markets at a price equal to marginal cost. That is,

\[
\frac{Sb}{4(1 + Sb)} < c < \frac{1}{b},
\]

where the first inequality is given by the condition \( w_i \geq c \) for any equilibrium\textsuperscript{18} and the second inequality is given by the condition \( Y(c) > 0 \). We analyze equilibria where the unit trade cost is sufficiently low to potentially permit cross-border trade in equilibrium.

In the subsequent analysis, we compare the outcome with cross-border trade to an equilibrium that is segmented, either due to a prohibitive trade cost or contracts that effectively allocate an exclusive territory to each distributor. In the segmented equilibrium, the manufacturing firm can set wholesale prices and fixed fees in each market to avoid a double-markup problem and to induce optimal retail prices. In this case the wholesale prices are, accordingly, equal to the marginal cost of production, i.e. \( w_i = c \), and the retail prices correspond to the prices set by an integrated monopolist, which are

\[
p^{ET}_A = \frac{1 + c}{2}, \quad (5)
\]
\[
p^{ET}_B = \frac{1 + bc}{2b}. \quad (6)
\]

We shall refer to this case as our benchmark equilibrium. In the segmented equilibrium, the retail price in market \( A \) exceeds the retail price in market \( B \), reflecting the less price-elastic demand in the former market. It follows that markets are naturally segmented for a sufficiently high \( t \geq \overline{t} \), where

\[
\overline{t} = \frac{1 - c}{2},
\]

We label trade costs above this level "prohibitive".

\textsuperscript{17}This is an important assumption for the results as we show in Ganslandt and Maskus (2007).

\textsuperscript{18}The binding constraint is given by the equilibrium wholesale price in market \( A \) under discriminatory wholesale pricing (given by equation 21) with a minimum at \( \overline{t}^D \) (given by equation 26).
3 Cross-border trade

3.1 The sub-game retail equilibrium

The next task is to analyze the effects of cross-border trade. Before we analyze the manufacturing firm’s optimal behavior it is useful to derive the sub-game retail equilibrium. A common feature of the three cases we shall analyze below is that market segmentation is imperfect. The manufacturing firm can neither directly nor indirectly impose exclusive territories. Recall that both distributors can sell in market $A$, while only the local distributor can sell in market $B$.

More precisely, in the retail sub-game the manufacturing firm has offered two contracts, $\{T_A, w_A\}$ and $\{T_B, w_B\}$, that have been accepted by the distributors. The distributors non-cooperatively set quantities in a Cournot-fashion in market $A$ and the local distributor chooses a profit-maximizing quantity in market $B$. The sub-game equilibrium in market $A$ is consequently given by the well-known Cournot output

$$x_A = \frac{1 - 2w_A + w_B + t}{3}$$

$$x_B = \frac{1 + w_A - 2w_B - 2t}{3}$$

subject to the condition that wholesale prices are such that equilibrium quantities are non-negative. Similarly, the sub-game equilibrium quantity in market $B$ is given by the monopoly solution

$$y_B = S \left(1 - \frac{bw_B}{2}\right).$$

The corresponding retail price in markets $A$ and $B$ are, respectively,

$$p_A = \frac{1 + w_A + w_B + t}{3},$$

$$p_B = \frac{1 + bw_B}{2b}.$$

For a sufficiently high trade cost, above a threshold denoted $\bar{t}$, parallel trade is unprofitable in equilibrium. In other words, the equilibrium is arbitrage-free. More precisely, cross-border trade is blocked if the manufacturing firm
sets wholesale prices that satisfy the no-arbitrage condition

\[
\frac{1 + w_A}{2} \leq w_B + t. \tag{13}
\]

and the sub-game retail equilibrium prices are

\[
p_A = \frac{1 + w_A}{2}, \tag{14}
\]

\[
p_B = \frac{1 + bw_B}{2b}. \tag{15}
\]

With this characterization we can now analyze the manufacturing firm’s behavior under different institutional assumptions. First, we consider wholesale price discrimination when the producer is allowed to set one different wholesale prices but is not permitted to restrict cross-border trade. Second, we study the effects of a policy requiring uniform pricing for both distributors.

### 3.2 Discriminatory Wholesale Pricing (D)

We start our analysis with wholesale price discrimination. For this purpose we assume that the manufacturing firm can set one price for each distributor. In this case the manufacturing firm has two instruments with which to solve three problems: inducing the profit-maximizing retail price in each market and ensuring an efficient global distribution by minimizing cross-border parallel trade, which wastes resources. Since the producer has too few instruments we shall expect inefficiencies and a sub-optimal outcome compared to exclusive territories.

The manufacturing firm set wholesale prices to maximize total profits

\[
\max_w X (w) (p_A (w) - c) + Y (w) (p_B (w) - c) - tx_B (w), \tag{16}
\]

where the last term on the right hand side is the resources used in trade from market B to A. Next, we find the equilibrium under two possible price-setting strategies: wholesale prices that permit PI and wholesale prices that block PI (we shall refer to the latter as arbitrage-free prices). We derive the optimal wholesale prices and compare the producer’s profit in both of these cases to find the more profitable strategy.

The optimal wholesale prices that permit cross-border trade can be found
by solving the following two first-order conditions with respect to \( w_A \) and \( w_B \)

\[
\frac{1 - 2w_A - 2w_B - 2t + 3c}{9} = 0, \tag{17}
\]

\[
\frac{1 - 2w_A - 2w_B - 2t + 3c}{9} + \frac{2t}{3} - \frac{Sb(w_B - c)}{2} = 0. \tag{18}
\]

The first term on the left hand side of both conditions is the pro-competitive effect in market \( A \) (which we term the horizontal externality between the competing distributors because it reduces the manufacturer’s profit). The second terms in both equations are the effects of costly cross-border trade (which we term inefficient distribution). The third term on the left hand side of the second condition, with respect to \( w_B \), is the double-markup problem in market \( B \) (which we term the vertical externality between the distributor and the manufacturing firm).

Note that for \( t = 0 \) the second terms are zero and the total number of problems for the manufacturing firm is two, the same as the number of instruments available. In this case the wholesale prices are perfect substitutes for inducing the profit-maximizing monopoly retail price in market \( A \). The optimal retail price in market \( B \) must, however, be induced solely with the wholesale price to the local distributor there. The unique wholesale price that solves the vertical externality equals the marginal cost of production. The manufacturing firm can thus obtain the same profit as a vertically integrated monopolist by combining the two wholesale prices to solve both the horizontal and vertical problems in this case.

If the trade cost is positive, however, there is an additional distortion that prohibits the manufacturing firm from obtaining the first-best outcome in retail markets. The manufacturing firm must therefore balance the trade-offs among the horizontal externality in market \( A \), the inefficiency in distribution and the vertical externality in market \( B \).

The severity of the problem with inefficient parallel trade increases in the trade cost. For a sufficiently high trade cost, above a threshold denoted \( \tilde{t}^D \) (derived below), it is profitable for the manufacturing firm to set arbitrage-free wholesale prices. These are prices that make cross-border trade unprofitable in equilibrium. Accordingly, to block PI the manufacturing firm sets wholesale prices that satisfy the no-arbitrage condition

\[
\frac{1 + w_A}{2} \leq w_B + t. \tag{19}
\]
The producer’s profit can be differentiated subject to this condition. We obtain the following first-order condition for wholesale prices that block parallel trade

$$\left(1 + c - 2w_B - 2t\right) - \frac{Sb(w_B - c)}{2} = 0,$$  \hspace{1cm} (20)$$

where the first term on the left hand side is the horizontal externality in market A and the second term is the vertical problem in market B. The first-order condition gives the profit-maximizing wholesale price in B while the wholesale price in A can be obtained from the no-arbitrage condition.

If we solve for the vectors of wholesale prices that permit and block PI we obtain the following result:

**Proposition 1** Assume that the trade cost is non-prohibitive and the producer can set one wholesale price for each distributor. Then the equilibrium wholesale prices are

$$w_A^D = \frac{1 + c - 4 + 5Sb}{2 - 2Sb} t \text{ and}$$  \hspace{1cm} (21)$$

$$w_B^D = \frac{c + 2t}{Sb} \text{ for } t \leq \overline{t}^D,$$  \hspace{1cm} (22)$$

$$w_A^D = \frac{2c(2 + Sb) + (2t - 1) Sb}{4 + Sb} \text{ and}$$  \hspace{1cm} (23)$$

$$w_B^D = \frac{2 + 2c + Scb - 4t}{4 + Sb} \text{ for } t > \overline{t}^D,$$  \hspace{1cm} (24)$$

and the equilibrium is unique.

The equilibrium volume of cross-border trade can be obtained by inserting the equilibrium wholesale prices for low trade costs \(t \leq \overline{t}^D\), given by (21), in equation (9). It follows that the volume of trade for \(t \leq \overline{t}^D\) is

$$x_B^D = \frac{1 - c}{2} - \frac{4 + 3Sb}{2Sb} t$$  \hspace{1cm} (25)$$

which decreases in the unit trade cost, \(t\). Parallel trade consequently occurs in equilibrium for low trade costs, while the equilibrium is arbitrage-free for higher trade costs. The threshold for arbitrage-free prices is

$$\overline{t}^D = \frac{(1 - c) Sb}{4 + 3Sb}$$  \hspace{1cm} (26)$$

which is strictly positive and below the prohibitive trade cost.
A closer look at the equilibrium reveals that the wholesale price in market $A$ first falls as trade cost increases in the low range ($t \leq \bar{t}^D$), then rises as the unit trade cost goes beyond the threshold level.\footnote{We derive retail prices in the next section, which discusses welfare results.} In contrast, the wholesale price in market $B$ first increases and then decreases. The result for the low-cost range ($t \leq \bar{t}^D$) is intuitive since the manufacturing firm would reduce the price in $A$ and raise the price in $B$ to moderate the negative effect of costly cross-border trade. This incentive becomes stronger as trade costs rise. Indeed, note from (21) that for a trade cost,

$$t > \bar{t}^S = \frac{(1 - c) Sb}{4 + 5 Sb},$$

where superscript $S$ refers to "subsidy", the manufacturing firm prefers to set a wholesale price in market $A$, i.e. $w_A$, that is below marginal cost. This would imply a decision to subsidize the distributor in market $A$, which would be profitable for the manufacturing firm because it makes that distributor more aggressive and reduces the volume of inefficient trade.

### 3.3 Uniform Wholesale Pricing (U)

In this section we derive the equilibrium under the assumption that the government forces the producer to charge a uniform wholesale price, $w_{AB}$, for both distributors. We again consider that the firm could set either a wholesale price that permits cross-border trade or one that deters it. In an equilibrium with parallel trade the wholesale price must solve this first-order condition

$$\frac{2 - 8w - 4t + 6c}{9} + \frac{t}{3} - \frac{Sb(w - c)}{2} = 0 \tag{28}$$

where the first term on the left hand side reflects the pro-competitive effect of trade in market $A$ (the horizontal externality), the second term is the effect of wasteful PI (the inefficiency in distribution) and the third term is the potential double-markup problem in market $B$ (the vertical externality).

For sufficiently high trade costs, above a threshold $\bar{t}^U$ (derived below), it is optimal to set an arbitrage-free wholesale price. In this case, the following condition must hold

$$w \geq 1 - 2t \tag{29}$$

This constraint is enough to ensure that the wholesale price is arbitrage-free.
and the distributor in \( B \) does not engage in PI. The equilibrium is presented in the following proposition:

**Proposition 2** Assume that the trade cost is non-prohibitive and the manufacturing firm sets a uniform wholesale price, i.e. \( w_A = w_B \). Then the equilibrium wholesale price is

\[
\begin{align*}
w^U_A &= w^U_B = \frac{4 + 9Scb + 12c - 2t}{9Scb + 16} \quad \text{for } t \leq t^U, \\
w^U_A &= w^U_B = 1 - 2t \quad \text{for } t > t^U,
\end{align*}
\]

and the equilibrium is unique.

Here, the wholesale price is a continuous decreasing function in the unit trade cost and the volume of parallel trade for \( t \) below the new threshold is

\[
x^U_B = \frac{(3Scb + 4)(1 - c) - (10 + 6Scb)t}{9Scb + 16}.
\]

The wholesale price is arbitrage-free for any trade cost greater than this threshold

\[
t^U = \frac{(1 - c)(4 + 3Scb)}{10 + 6Scb}.
\]

Further, note that \( t^U > t^D \), which shows that PI exist in equilibrium for higher trade costs than with discriminatory wholesale prices. The intuition for this is that it is relatively more expensive for the producer to use the uniform wholesale price to reduce the volume of parallel trade. If the manufacturing firm is required to set a uniform price and it increases that price for intermediate and high trade costs, the result is a double-markup problem in both retail markets. The vertical control problem is consequently more difficult to solve with a uniform price than with a discriminatory price.

### 4 Welfare

In this section we analyze consumer surplus and welfare under discriminatory and uniform pricing. For this purpose we define welfare as the sum of aggregated consumer surplus in both markets plus the manufacturing firm's profit. Consumer surplus is uniquely determined by the retail prices. For a given trade cost and a given marginal cost of production, the manufacturing firm's profit is uniquely determined by retail prices and the volume of cross-border trade.
From a welfare perspective the most interesting variables are, consequently, the retail prices and the level of parallel imports.

Two conclusions highlight our results. First, for trade costs above a threshold \( t \) (computed below), the policy of requiring a uniform wholesale price is Pareto-dominated by market segmentation. The reason is that uniform wholesale prices generate higher retail prices in both markets while reducing firm profits. This suggests that the policy of not permitting price discrimination, designed to safeguard wholesale competition, easily could have the unintended consequence of reducing economic well-being. However, at low trade costs, below the threshold \( t' \) (computed below), the uniform-price policy can generate gains in consumer welfare. Thus, it seems that uniform pricing and policies taken to reduce transactions costs, such as harmonized product standards, could be complementary.

The welfare rankings between uniform and discriminatory wholesale pricing are more complex. We describe here the interesting and relevant case where markets differ substantially in demand elasticity (e.g., a high value for \( b \)), which ensures that the retail price in market \( B \) is below the retail price in market \( A \). We consequently assume that \( b \) is above a threshold \( b' \), given by

\[
\frac{b}{1 + c} = \frac{2}{1 + c}.
\]

This situation could characterize market conditions when low-income Eastern European economies join the high-income existing EU members and parallel trade is unrestricted. In this case we show that the restraint of a uniform wholesale price diminishes joint consumer welfare for a unit trade cost above the threshold \( t' \).

To establish these results we first derive the retail prices in the discriminatory pricing equilibrium. We insert the equilibrium wholesale price \( w_A \) from the two ranges of trade costs noted in equations (21) and (23) into equation (11), and that for \( w_B \) in (22) and (24) into (12), to obtain

\[
\begin{align*}
P^D_A &= \frac{1 + c - t}{2} \quad \text{and} \\
P^D_B &= \frac{S + Scb + 2t}{2bS} \quad \text{for } t \leq t^D, \\
P^D_A &= \frac{2 + tSb + 2c + Scb}{4 + Sb} \quad \text{and} \\
P^D_B &= \frac{1}{2b} + \frac{2 + 2c + Scb - 4t}{2(4 + Sb)} \quad \text{for } t > t^D,
\end{align*}
\]
which are continuous functions in the unit trade cost with kinks at the critical threshold for arbitrage-free prices, $\bar{T}^D$. For illustrative purposes we have plotted retail prices as functions of the unit trade cost in Figure 1. We also show the volume of parallel trade, $x_{pB}^D$.

Note that as the unit trade cost falls from the level supporting exclusive territories (ET), the gap between retail prices narrows for this intermediate range of trade costs as the manufacturer strives to block costly cross-border trade. Accordingly, the threat of parallel trade results in retail price convergence to some extent, arising from the firm’s inability fully to manage the vertical control problem. Once the trade cost falls below the threshold we find that retail prices actually move apart, a result consistent with that in Ganslandt and Maskus (2007). This stems from the incentive to set different wholesale prices (with that in $A$ rising and that in $B$ falling as $t$ declines) in order to minimize the horizontal externality in the import market, even as the volume of PI goes up.

![Figure 1: Retail prices with discriminatory wholesale pricing ($S = 1, b = 2, c = 1/4$)](image-url)
Next, we derive the retail prices in the uniform pricing equilibrium. We insert the optimal wholesale price given by (30) and (31) in the sub-game equilibrium (11) and (12) to obtain the retail prices

\[ p_A^U = \frac{1 + t}{3} + \frac{2}{3} \left( \frac{4 + 9Scb + 12c - 2t}{9Sb + 16} \right) \]  
and

\[ p_B^U = \frac{1}{2b} + \frac{1}{2} \left( \frac{4 + 9Scb + 12c - 2t}{9Sb + 16} \right) \]  
for \( t \leq \bar{t}^U \),

\[ p_B^U = 1 - t \]  
and

\[ p_B^U = \frac{1}{2b} + \frac{1}{2} - t \]  
for \( t > \bar{t}^U \),

with kinks at the threshold for the arbitrage-free price in this case. The retail prices as functions of the unit trade cost under uniform wholesale pricing are illustrated in Figure 2.

There are two interesting features of this equilibrium. First, a uniform wholesale price results in retail prices above the segmented price in both markets for
intermediate and high trade costs (and in market \( B \) throughout the range). It is optimal for the manufacturing firm to set a wholesale price that results in a double-markup problem in both markets in order to minimize the waste of resources in PI. Second, the volume of cross-border trade with a uniform wholesale price is a decreasing function in \( t \). The gap between retail prices in markets \( A \) and \( B \) is relatively narrow for low trade costs and relatively wide for higher trade costs. A policy that requires the manufacturing firm to set non-discriminatory wholesale prices will thus have a pro-competitive effect in market \( A \) for low trade costs and the effect is some degree of price integration.

More specifically, retail prices in both markets are above the segmented levels, i.e. \( p_{UA}^U \geq p_{A}^{ET} \) and \( p_{UB}^U \geq p_{B}^{ET} \), if \( t \) is above

\[
\hat{t}_1 = \frac{3Sb(1 - c)}{6Sb + 8},
\]  

(43)

and, correspondingly, retail prices in both markets are above the discriminatory levels, i.e. \( p_{UA}^U \geq p_{A}^D \) and \( p_{UB}^U \geq p_{B}^D \), if \( t \) is above

\[
\hat{t}_2 = \frac{(7Sb + 8)(1 - c)}{28 + 17Sb},
\]  

(44)

both of which are below the prohibitive trade cost \( \bar{t} \) given by equation (7). Taking the maximum of the two thresholds, i.e.

\[
\hat{t} = \max(\hat{t}_1, \hat{t}_2).
\]  

(45)

we obtain the following result

**Proposition 3** Let \( b > b_0 \). If the trade cost is above the critical level given by equation (45) and below the prohibitive level given by equation (7), i.e. \( \hat{t} < t < \bar{t} \), then the uniform wholesale pricing equilibrium is Pareto-dominated by both exclusive territories and discriminatory wholesale pricing, i.e. \( p_{UA}^U > p_{A}^{ET} > p_{A}^D \) and \( p_{UB}^U > p_{B}^{ET} > p_{B}^D \) and \( \pi^U < \pi^D < \pi^{ET} \).

Next we proceed to analyze total surplus. The aggregated consumer surplus is

\[
CS = \left[ \left( X - \frac{X^2}{2} \right) - p_A X \right] + \left[ \frac{1}{6} \left( Y - \frac{Y^2}{2S} \right) - p_B Y \right],
\]  

(46)

where the first term is consumer surplus in \( A \) and the second term is consumer surplus in \( B \). We insert the demand functions in markets \( A \) and \( B \) to get consumer surplus as a function of the retail prices:

\[
21
\]
\[ CS(p) = \frac{1}{2} (1 - p_A)^2 + \frac{S}{2b} (1 - bp_B)^2 \]  

which is continuous, concave and decreasing in both \( p_A \) and \( p_B \). The aggregated consumer surplus values under price discrimination and under a uniform wholesale price are summarized in Table 1.

**Table 1: Total consumer surplus, CS**

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Formula</th>
</tr>
</thead>
</table>
| Discriminatory pricing, \( t \leq t^D \) | \[
\frac{1}{2} (1 - \left( \frac{1}{2} + \frac{1}{2}c - \frac{1}{2}t \right))^2 + \frac{S}{2b} \left( 1 - b \left( \frac{1}{2b} \left( \frac{S + Sc + 2t}{S} \right) \right)^2 \right)
\] |
| Discriminatory pricing, \( t > t^D \) | \[
\frac{1}{2} \left( 1 - \left( \frac{2 + 8b + 2c + Sc}{4 + 8b} \right) \right)^2 + \frac{S}{2b} \left( 1 - b \left( \frac{4 + 8b + 2c + Sc}{2(4 + 8b)b} \right) \right)^2
\] |
| Uniform pricing, \( t \leq t^U \)    | \[
\frac{1}{2} \left( 1 - \left( \frac{3b + 8 + 6Sc + 8c + 4 + 3Sc}{9b + 16} \right) \right)^2 + \frac{S}{2b} \left( 1 - b \left( \frac{9b + 16 + 4b + 9Sc + 12c + 8b}{(9b + 16)b} \right) \right)^2
\] |
| Uniform pricing, \( t > t^U \)    | \[
\frac{1}{2} (1 - (1 - t))^2 + \frac{S}{2b} \left( 1 - b \left( \frac{1+b-t}{2} \right) \right)^2
\] |

Total consumer surplus functions under discriminatory and uniform wholesale pricing are illustrated in Figure 3. The aggregated consumer surplus under discriminatory pricing has its maximum for intermediate trade costs, where the retail price gap is relatively narrow. The allocation in the retail markets is accordingly relatively efficient for the intermediate range of trade costs. The allocative inefficiency increases and consumer surplus decreases in the retail price gap. The minimum consumer surplus under discriminatory wholesale pricing accordingly occurs for zero and prohibitive trade costs, when the equilibrium retail prices are identical to the retail prices in a segmented equilibrium.

In the uniform wholesale pricing equilibrium, the aggregated consumer surplus has its maximum when the trade cost is zero due to the price-integrating effect of cross-border trade in that case. Aggregated consumer surplus has its minimum at the threshold for an arbitrage-free wholesale price, which is close
to the prohibitive trade cost. At this point the double-markup problems in both markets are most severe and the resulting retail prices are above the prices in a segmented equilibrium, while the retail price gap is just as wide as in the segmented equilibrium. There are consequently no offsetting benefits of price integration.

$\text{Figure 3: Total consumer surplus with discriminatory and uniform wholesale pricing ($S = 1, b = 2, c = 1/4$)}$

Wholesale price discrimination dominates the uniform wholesale price for intermediate and high trade costs ($t \geq t'$), while the uniform price dominates for low trade costs ($t < t'$). The critical threshold is

$$t' = \frac{Sb(1-c)}{8 + 5Sb}.$$  \hspace{0.5cm} (48)

Consumers are consequently better off as a group with uniform wholesale pricing if the unit trade cost is low. The intuition for this is straightforward. Cross-
border trade has both a pro-competitive and price-integrating effect for low trade costs. The narrow gap between retail prices in the two markets has a positive effect on total consumer surplus due to a relatively moderate allocative distortion compared to that under discriminatory prices.

We have assumed that markets differ noticeably in demand elasticity (eq. 34) and this assumption ensures that the retail price in market \( B \) is below the retail price in market \( A \) in any equilibrium. This is also a sufficient condition for the consumer surplus under discriminatory pricing to be higher than under exclusive territories, i.e. \( CS^D \geq CS^{ET} \), for any trade cost. We can combine these two findings to obtain the following result:

**Proposition 4** Let \( b > \frac{1}{2} \). If the trade cost is strictly positive and below the critical threshold given by equation (48), i.e. \( t < t' \), consumer surplus is higher under uniform wholesale pricing than under discriminatory wholesale pricing and exclusive territories, i.e. \( CS^U > CS^D \geq CS^{ET} \).

Having considered consumer surplus we now proceed to compute the equilibrium profit for the manufacturing firm. We insert wholesale prices in equation (16) to obtain the profit under discriminatory and uniform wholesale pricing. The manufacturing firm’s profit under price discrimination and a uniform wholesale price is summarized in Table 2.

### Table 2: The manufacturing firm’s profit

| Profit Formula                  | Discriminatory wholesale pricing, \( t \leq \tilde{t}^D \): | |
|-------------------------------|-----------------------------------------------------------------|
| \( \frac{S}{4b} + \frac{1+bsc^2-2sc-2c+c^2}{4} + t \left( \frac{5bs+4t-2bs+2sc}{4bs} \right) \) | |
| Discriminatory wholesale pricing, \( t > \tilde{t}^D \): | |
| \( \frac{bs(1-c-t)}{4+bs} + \frac{(1-2cb+c^2b^2)}{4b}S + \frac{(1-c)^2}{4+bs} \) | |
| Uniform wholesale pricing, \( t \leq \tilde{t}^U \): | |
| \( \frac{S(1-2bc)}{4b} + \frac{16+16c^2+8bs-16scb+24sc^2b-32c+9c^2b^2}{4(9bS+16)}S^2 + t \left( \frac{5bs+9t-4+4c-2bs+2scb}{9bS+16} \right) \) | |
| Uniform wholesale pricing, \( t > \tilde{t}^U \): | |
| \( (1-c-t) + \frac{S(1+b-2bt-2b)}{4b}t + \frac{S(1+b-2bt-2b)(1-b+2bt)}{4b} \) | |

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Profits under discriminatory and uniform wholesale pricing are illustrated in Figure 4. The profit of the manufacturing firm is higher under discriminatory pricing than uniform pricing for obvious reasons. The firm has one more instrument to solve the three problems it faces, and it can accordingly set prices that result in less parallel trade and retail prices closer to the optimal level compared to the constraint it operates under with the uniform wholesale pricing equilibrium.

The firm’s profit is a U-shaped function in the trade cost under both discriminatory and uniform wholesale pricing. The profit function under discriminatory wholesale pricing has its minimum at a relatively low trade cost, i.e.

\[ t = \frac{bS(1-c)}{5bS + 4} \] (49)

At this point the total resources used in cross-border trade are significant and the inefficiency in distribution is substantial. Under uniform wholesale pricing this point is at a higher trade cost, i.e.

\[ t = \frac{(1-c)(2+bS)}{5bS + 9} \] (50)

and the minimum for this profit function is accordingly at an intermediate trade cost.

Total welfare, the sum of consumer surplus and the manufacturing firm’s profit, is illustrated in Figure 5. It is evident that the requirement not to discriminate in wholesale prices generates higher welfare only at low trade costs.

The consumer surplus and the profit of the manufacturing firm allow us to analyze the interaction between competition policy and trade costs, particularly for low \( t \). For this purpose we take the derivative of consumer surplus under uniform wholesale pricing for \( t \leq t_U \), which is

\[ \frac{dCS^{U}}{dt} = \frac{-Sb(4-3c) - 4(1-c) + S + 2t(Sb+1)}{2(9Sb + 16)} \] (51)

and, correspondingly, the derivative of the profit under uniform wholesale pricing for \( t \leq t_U \), which is

\[ \frac{d\pi^{U}}{dt} = \frac{-4(1-c) - 2Sb(1-c) + 2t(5bS + 9)}{9Sb + 16} \] (52)

Both derivatives are negative for low trade costs, implying that consumer surplus
and profits rise as the unit trade cost \((t)\) diminishes. We conclude that a market-integration policy that reduces trade and transactions costs is complementary from a welfare perspective to a competition policy that requires firms with significant market power to charge non-discriminatory wholesale prices.

5 Extensions

The analysis above is based on two important assumptions. One was that, under the discriminatory wholesale pricing regime, the marginal cost of production is sufficiently high to permit the manufacturing firm to subsidize the distributor in market \(A\) with a wholesale price below the marginal cost of production for some trade costs. Another was that retail markets are segmented. We assumed that the distributor (or his agent) is prohibited from buying the good in one retail market and shipping it to the other market. In this section we extend our analysis by relaxing both these assumptions.
Figure 5: Welfare with discriminatory and uniform wholesale pricing ($S = 1, b = 2, c = 1/4$)

5.1 Wholesale Pricing at or above Marginal Cost (C)

We noted above that for some trade costs the manufacturing firm has a strategic incentive to subsidize the local distributor in the import market in order to make it more aggressive and take market share from the importing distributor. This subsidization involves a wholesale price that is below the marginal cost of production.

Now consider the possibility that the manufacturing firm cannot subsidize the distributor in market $A$. For instance, the competition authorities may impose a restriction that the manufacturing firm must charge a wholesale price that covers its marginal cost of production or the marginal cost of production may be close to zero, thus restricting the scope for subsidization. This might be called a policy of "non-exclusionary" pricing for it precludes the manufacturer from subsidizing one distributor to the exclusion of the other.

The optimal wholesale price in market $B$ that permits parallel trade can be found by solving the first-order condition subject to the binding restriction
\[ w_A = c, \text{ i.e.} \]
\[
\frac{1 + c - 2w_B - 2t}{9} + \frac{2t}{3} - \frac{Sb(w_B - c)}{2} = 0, \quad (53)
\]
where the wholesale price in \( A \) is simply replaced by the marginal cost of production. Since the binding restriction on the wholesale price in market \( A \) pushes that price above the optimal level, the manufacturing firm must use the wholesale price in market \( B \) to reduce the volume of cross-border trade. This forces the manufacturing firm to charge a higher price to the local distributor in \( B \), which exacerbates the double-markup problem there.

For sufficiently high trade costs, above the critical threshold \( \bar{t}^C \), it is optimal for the manufacturing firm to block cross-border trade. Arbitrage-free wholesale prices must satisfy the following condition

\[ w_B \geq \frac{1 + c - 2t}{2} \quad (54) \]

and we have the following result:

**Proposition 5** Assume that the trade cost is non-prohibitive and wholesale prices must be above or equal to the marginal cost of production. Then the equilibrium wholesale prices are

\[
w_A^C = \max \left( \frac{1 + c - \frac{4 + 5Sb}{2Sb}t}{2}, c \right) \quad (55)
\]
\[
w_B^C = \min \left( \frac{c + \frac{2t}{Sb} + \frac{2c + 8t + 9Scb}{4 + 9Sb}}{Sb}, \frac{1 + c - 2t}{2} \right) \quad (56)
\]

and the equilibrium is unique.

The assumption that wholesale prices must be non-exclusionary is binding for intermediate and high trade costs, \( t \geq \bar{t}^S \), given by (27). In the intermediate range the volume of parallel trade is

\[ x_B^C = \frac{3Sb (1 - c) - (8 + 6Sb) t}{4 + 9Sb} \quad (57) \]

which is strictly more than the volume of such trade when the manufacturing firm sets a subsidized price to the distributor in market \( A \). This is not surprising since the manufacturing firm essentially lost one control instrument \( w_A \). Parallel trade consequently occurs in equilibrium for a wider range of trade costs.
The threshold for arbitrage-free prices is now

\[ \overline{t}^C = \frac{3(1-c)Sb}{2 + 3Sb} \]  \hspace{1cm} (58)

which is strictly higher than the threshold with price discrimination (\( \overline{t}^D \)). The effect of a policy that bans subsidies by precluding wholesale prices below marginal cost is, consequently, an increased volume of PI for a wider range of trade costs.

We insert the equilibrium wholesale prices (55) and (56) into the sub-game equilibrium (11) and (12) to obtain the retail prices as functions of the unit trade cost and the volume of cross-border trade, which are illustrated in Figure 6.

For high trade costs, i.e. \( t > \overline{t}^C \), wholesale prices that are at or above marginal cost are Pareto-dominated by discriminatory wholesale pricing. Consumers in market A, consumers in market B and the manufacturing firm are
all worse off. This result stems from the manufacturing firm’s market power. A restriction on prices in a market with imperfect competition can generate significant distortions that make the equilibrium substantially less efficient. In our case the manufacturing firm must use the wholesale price in market $B$ to reduce the scope for costly cross-border trade. The effect is that the retail prices increase in both markets. Consumption accordingly moves away from what would be the first-best solution for the manufacturing firm, i.e. the segmented equilibrium, and both consumers and the manufacturing firm lose as a result.

5.2 Retail Arbitrage

We initially assumed that retail markets are segmented. While we think this is a relevant assumption in many cases, readers may wonder about the implications of retail arbitrage in the model. For this purpose, consider the possibility that the distributor in market $A$ (or an agent) can import the product from market $B$. Arbitrage by distributor $A$ (in which he buys at the retail level abroad in order to find a cheaper source of supply than the available wholesale price) is not profitable if the margin between the wholesale price in market $A$ and the retail price in market $B$ is lower than the unit trade cost $t$. Formally, the no-arbitrage condition is

\[ w_A \leq p_B + t \]  \hspace{1cm} (59)

and in order to determine whether this condition is slack in equilibrium we insert the accommodation wholesale price in market $A$ and the retail price in market $B$. The critical threshold for retail markets to be segmented in this case is

\[ \tilde{t}^R = \frac{S (b - 1)}{6 + 7Sb} \]  \hspace{1cm} (60)

which is close to zero for $b$ close to 1. Markets are consequently segmented at the retail level by the natural barrier $t$ for intermediate and high trade costs, i.e. $t \geq \tilde{t}^R$. However, if markets are different in terms of price elasticity, then retail arbitrage would limit the scope for price discrimination at low trade costs, i.e. $t < \tilde{t}^R$.

A second possibility might be arbitrage by final consumers. However, perfect consumer retail arbitrage is a strong assumption and inconsistent both with the fact that the bulk of PI occurs at the distributor level and with persistent differences in retail prices within the EU. There are good reasons to expect limited arbitrage of this kind even without restrictions on parallel trade. First, as noted
above there are likely to be complementarities in retail services that cannot be
provided by arbitrageurs. Second, there may be significant fixed costs in organ-
zizing cross-border retail trade. Third, there may be large information costs
for consumers in determining product prices and characteristics for purposes of
organizing arbitrage. Thus, we think our analysis of distributor-level PI is valid
in the bulk of realistic circumstances.

6 Two-Way Cross-Border Trade

In this section we modify our model and permit two-way parallel trade. Thus,
we analyze the possibility of PI into market A from market B and vice versa.
We restrict our attention to the cases of wholesale price discrimination and
an enforced uniform wholesale price. The distributors non-cooperatively set
quantities in a Cournot fashion in the two markets. A sub-game equilibrium in
market B with cross-border trade from A to B is therefore

\[ y_A = \frac{S(1 + w_B b - 2w_A b - 2tb)}{3}, \]

\[ y_B = \frac{S(1 - 2w_B b + w_A b + tb)}{3}, \]

while the sub-game equilibrium in A, with cross-border trade from B to A,
is given by the optimal quantities (8) and (9). The manufacturing firm sets
wholesale prices to maximize total profits

\[ \max_w X(w)(p_A(w) - c) + Y(w)(p_B(w) - c) - t(x_B(w) + y_A(w)), \]

where the last term on the right-hand side is the resources used in cross-border
trade.

First, consider wholesale price discrimination. Prices block arbitrage from
A to B if

\[ p_B \leq w_A + t \]

for then cross-border trade in that direction would be unprofitable. It follows
that the manufacturing firm can set the discriminatory wholesale prices given
by (21) and (22), for sufficiently low trade costs, since these prices would block
trade from A to B. More specifically, these prices are arbitrage-free as long as
the trade cost is below the threshold

$$\tilde{T}_2^p = \frac{(b - 1) S}{6 + 3Sb}. \quad (65)$$

Above this threshold two-way trade could potentially occur. However, it remains profitable for the manufacturing firm to set wholesale prices that actually eliminate trade from A to B. Indeed, permitting two-way trade can never be profitable if the manufacturing firm can set discriminatory wholesale prices. If two-way arbitrage occurred the manufacturing firm could induce the same retail prices (remember that wholesale prices are perfect substitutes for this purpose) and reduce the total volume of cross-border trade by increasing \(w_A\) and decreasing \(w_B\). Thus, two-way parallel trade does not occur in equilibrium with discriminatory prices. Accordingly, the producer chooses wholesale prices that are arbitrage-free and solve the following equation

$$\frac{S (1 + w_B b - 2w_A b - 2tb)}{3} = 0. \quad (66)$$

It follows that the first-order condition is

$$\frac{b - 1 - 3w_B b + 3cb}{6b} - \frac{Sb (w_B - c)}{2} + \frac{t}{2} = 0 \quad (67)$$

where the first term reflects the horizontal externality in market A, the second term reflects the vertical externality in market B and the third term reflects the inefficiency in distribution. The optimal wholesale prices are

$$w_A = \frac{2 + b + 3Sb}{6b(Sb + 1)} + \frac{c}{2} - \frac{1 + 2Sb}{2(Sb + 1)} t, \quad (68)$$

$$w_B = \frac{b - 1}{3b(Sb + 1)} + \frac{t}{(Sb + 1)} + c. \quad (69)$$

In this situation there remains one-way parallel trade from B to A and its volume decreases in \(t\), becoming zero if the trade cost is above the threshold

$$\tilde{T}_2^p = \frac{2 + 2b^2 S + b + Sb - 3Sb^2 c - 3bc}{3b (3 + 2Sb)}. \quad (70)$$

For trade costs above this threshold, the manufacturing firm can block trade in both directions. It sets wholesale prices such that \(x_A = 0\) and \(y_B = 0\), where \(x_B\) is given by equation (9) and \(y_A\) is given by equation (61). The optimal
wholesale prices are

\[ w_A = \frac{2 + b - 6tb}{3b}, \quad (71) \]
\[ w_B = \frac{1 + 2b - 6tb}{3b}. \quad (72) \]

Finally, two-way trade is blocked for high trade costs and the discriminatory prices (23) and (24) comprise the equilibrium. The threshold for this outcome is

\[ t^{D2}_3 = \frac{4 + 2b - 6cb - 3Sb^2c + Sb + 2Sb^2}{6b(2 + Sb)} \quad (73) \]

above which two-way cross-border trade is no longer a binding restriction for the manufacturing firm.

The wholesale and corresponding retail prices under wholesale price discrimination and two-way trade are illustrated in Figure 7. Two-way parallel trade changes the equilibrium wholesale prices for intermediate trade costs between the thresholds \( t^{D2}_1 \) and \( t^{D2}_2 \).

Next, consider the equilibrium with a uniform wholesale price. In this case two-way trade is potentially profitable for low trade costs. The first-order condition for the manufacturing firm is

\[ \frac{2 - 8w - 4t + 2c}{9} + \frac{t(1 + Sb)}{3} + \frac{2S(1 - 4wb - 2tb + 3cb)}{9} = 0 \quad (74) \]

and the optimal wholesale price is

\[ w = \frac{2 + 6c + 2S + 6Scb - t - tSb}{8(1 + Sb)} \quad (75) \]

and the equilibrium is unique. The volume of trade from \( A \) to \( B \), i.e. \( y_A \), decreases in \( t \) and for sufficiently high trade costs it is zero. The critical threshold is

\[ t^{U2}_1 = \frac{2(4 + 3Sb - b - 3bc - 3Sb^2c)}{15(1 + Sb)b} \quad (76) \]

Above this threshold, the manufacturing firm consequently blocks trade from \( A \) to \( B \) by solving

\[ y_A = \frac{S(1 + wb - 2wb - 2tb)}{3} = 0 \quad (77) \]
Figure 7: Wholesale and retail prices with price discrimination and two-way parallel trade ($S = 1, b = 2, c = 1/4$) and setting a wholesale price equal to

$$w = \frac{1}{b} - 2t. \quad (78)$$

This wholesale price quickly approaches the optimal uniform wholesale price with one-way trade, given by equation (30), from above and the two are equal at the threshold

$$t^U_2 = \frac{9Sb + 16 - 9Sb^2c - 12bc}{6b(5 + 3Sb)}. \quad (79)$$

Above this threshold, trade from $A$ to $B$ is blocked by the unit trade cost and the manufacturing firm can set the same uniform wholesale price as with one-way trade, i.e. the equilibrium given by (30) and (31). The wholesale price is arbitrage-free for any trade cost greater than

$$\tilde{t}^U_3 = \tilde{t}^U = \frac{(1 - c)(4 + 3Sb)}{10 + 6Sb}. \quad (80)$$
The uniform wholesale price and the corresponding retail prices are plotted in Figure 8. It is worth noting that for \( t < \frac{t_1}{2} \) retail prices are higher in both markets with two-way trade compared to the retail prices with one-way trade, \( p_{A}^{U} \) and \( p_{B}^{U} \) (not shown in Figure 8). Here, the restriction that there be a single uniform price makes it yet harder for the manufacturer to limit the cost of parallel trade, now happening in both directions, thereby pushing up retail prices even more.

![Figure 8: Retail prices and the uniform wholesale price with two-way parallel trade \((S = 1, b = 2, c = 1/4)\)](image)

7 Conclusion

We developed a model in which a manufacturing firm owns an intellectual property right in two markets but its ability to limit parallel imports from one market to the other is exhausted. In this environment, the firm has the ability to set wholesale prices - either discriminatory or uniform depending on the regulatory regime - to its independent distributors in the two locations. It will use
its available instruments to maximize profits within the vertical price control framework. There are three essential trade-offs for the manufacturer. It wishes to restrict the extent of competition from PI in market A (a horizontal externality), limit the amount of trade because it wastes real resources in transport costs (inefficient distribution), and avoid the double-markup problem in market B arising from the inability to set an efficient wholesale price (a vertical externality).

We considered two principal policy regimes: a discriminatory pricing regime permitting varying wholesale prices for each distributor and a uniform pricing regime forcing the manufacturing firm to set a common wholesale price for all distributors. We also analyze a regime that requires the manufacturing firm to set wholesale prices that cover the marginal cost of production.

Our analysis turned up some interesting results. The equilibrium analysis shows that discriminatory pricing, on the one hand, may result in partial retail price divergence for low and high trade costs. The incentive to minimize the resources wasted in trade activities by reducing the retail price gap between markets counteracts the underlying incentive to induce different retail prices in the two markets. The problem with inefficient distribution is particularly severe for intermediate trade costs since the trade barrier does not block PI but reduces revenues significantly. Uniform pricing, on the other hand, results in retail prices higher than the monopoly level for high trade costs, close to the prohibitive level. For high trade costs the manufacturing firm has a strong incentive to impede PI, but in order to achieve this goal the firm must raise retail prices in both markets. In contrast, for low trade costs it results in price convergence as well as a pro-competitive effect in the import market. The manufacturing firm is willing to accept a larger volume of parallel imports and the pro-competitive effect can accordingly be substantial.

The welfare analysis shows that, depending on circumstances, either discriminatory pricing or uniform pricing may be more beneficial. This finding has important implications for competition policy. A regulation that makes price discrimination illegal \textit{per se}, if it impedes parallel imports, may not be optimal. Requiring the manufacturing firm to charge a uniform wholesale price may be optimal for low trade costs when the pro-competitive effect is substantial but may have a severe negative effect on consumer welfare when trade costs are high as the primary effect is that retail prices increase in all markets. Further, when there is a possibility of two-way parallel trade the uniform-price restriction can raise retail prices at even low trade costs. These consequences, presumably
unintended, of the pricing restraint suggests that an effects-based approach in competition policy is advisable under these circumstances.

Finally, the welfare analysis show that market integration and competition law may be important complements in a policy perspective. This complementarity works both ways for low and intermediate trade costs. A reduced unit trade cost makes uniform pricing more attractive for consumers. Correspondingly, adopting a uniform pricing regime enhances the welfare incentives to continue the gradual dismantling of trade barriers.
References


